

# Preliminary Investigation

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Caltrans Division of Research, Innovation, and System Information

Produced by Hamid Sadraie

## *Development of a Validated Methodology for Seismic Analysis and Design of Standard and Pile-Supported Retaining Walls*

Requested by Charles Sikorsky

Date March 17, 2015

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### Executive Summary

Caltrans currently uses a force-based method for the seismic analysis and design of standard retaining walls. Preliminary studies show that this method is overly conservative. In addition, Caltrans does not have any guideline for the seismic analysis and design of pile-supported retaining walls. As a result, research is needed to establish a new method for the seismic analysis and design of standard and pile-supported retaining walls. The new method is deemed to be a displacement-based method. It should be readily applicable to Caltrans' practice. It should be also validated with existing experimental data sets, and verified against detailed finite element models.

## 1. Background

Earth retaining structures are an essential component of the transportation infrastructure. The analysis and design of earth retaining structures in California is currently based on AASHTO Load and Resistance Factor Design (LRFD) Bridge Design Specifications along with the corresponding California Amendments [Appendix A]. This analysis and design approach uses a force-based method to accommodate seismic loads. In a force-based method, the structure is designed to have enough capacity to resist peak earthquake loads [Anderson et al., 2008]. Such criterion, except for highly brittle structures, is overly conservative and implies additional costs for Caltrans in comparison with displacement-based criteria [Kavazanjian et al., 2011].

The conservative philosophy of a force-based method does not consider the transient nature of earthquake loads and that the duration of peak earthquake loads is short in comparison with permanent gravity loads. In reality, it is allowable to have substantial yielding in a ductile structure under extreme loads. Yielding will modify the dynamic behavior of the structure in a way that a reduction in the force demand from the assumed elastic behavior will be acceptable [Kavazanjian et al., 2011]. Another consequence of yielding will be an increase in the fundamental period of the structure. As the fundamental period of the structure elongates, forces will usually decrease while displacements will usually increase [Kavazanjian et al., 2011].

A displacement-based method is the alternative to Caltrans' current approach to the analysis and design of earth retaining structures. In a displacement-based method, the structure is allowed to slide during extreme events [Anderson et al., 2008]. As a result, a reduction in seismic loads is acceptable. Research is needed to establish a new displacement-based method for the seismic analysis and design of standard retaining walls. In addition, the new method should offer guidelines for the seismic analysis and design of pile-supported retaining walls. It should be also validated with existing experimental data sets, and verified against detailed finite element models.

## 2. Summary of Findings

Caltrans' current approach to the seismic analysis and design of standard retaining walls is overly conservative. In addition, Caltrans does not have any guideline for the seismic analysis and design of pile-supported retaining walls. The new method which will be established through this research study should be readily applicable to Caltrans' practices. Therefore, it should consider a broad range of retaining walls which Caltrans currently uses. Some examples are depicted in Figures 1, 2, and 3 [Shamsabadi et al., 2013].



Figure 1. Semi-gravity cantilever walls (reproduced from [Shamsabadi et al., 2013])

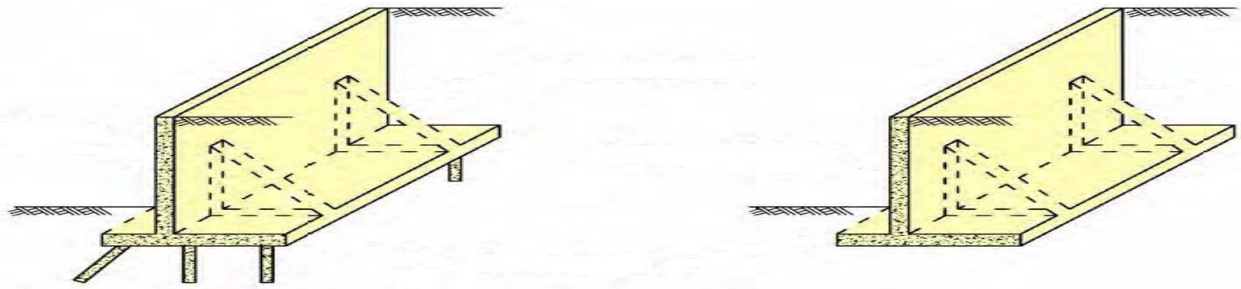


Figure 2. Counterfort walls (reproduced from [Shamsabadi et al., 2013])

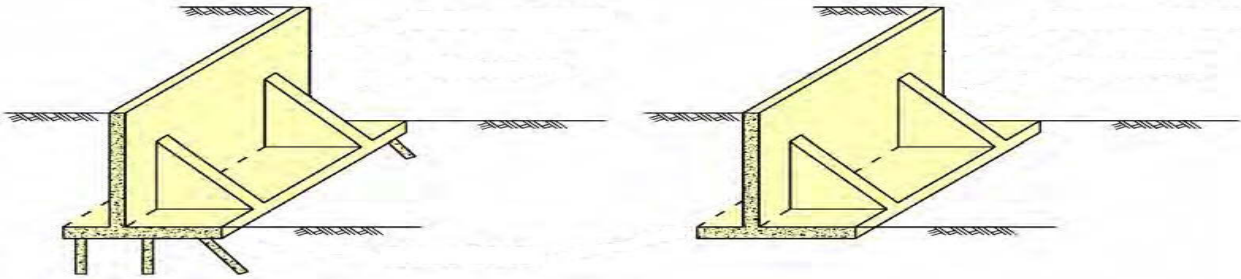


Figure 3. Buttressed walls (reproduced from [Shamsabadi et al., 2013])

The current analysis and design of retaining walls in California use a force-based method to accommodate seismic loads. In this method, the dynamic soil pressure is represented by pseudo-static forces which are calculated through either the Mononobe-Okabe method or the trial wedge method [Appendix A]. As it is shown in Figures 4, 5, 6, and 7, the soil failure in both methods is assumed to happen on a planar surface. The details of the two methods and the definitions of the parameters in Figures 4, 5, 6, and 7 are explained in [Shamsabadi et al., 2013].

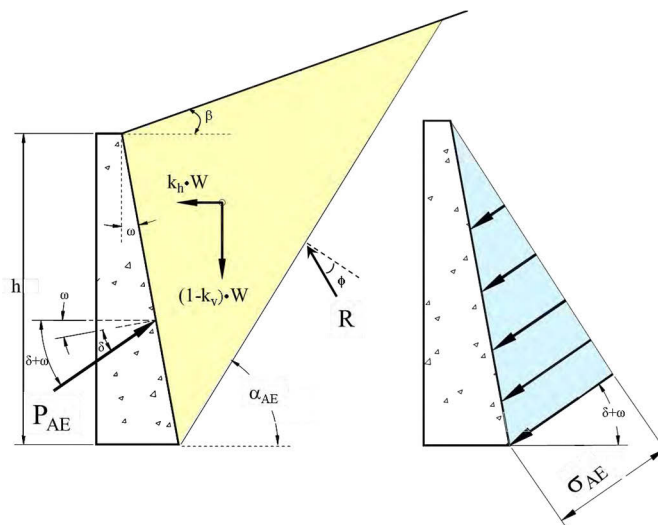


Figure 4. Mononobe-Okabe active pressure (reproduced from [Shamsabadi et al., 2013])

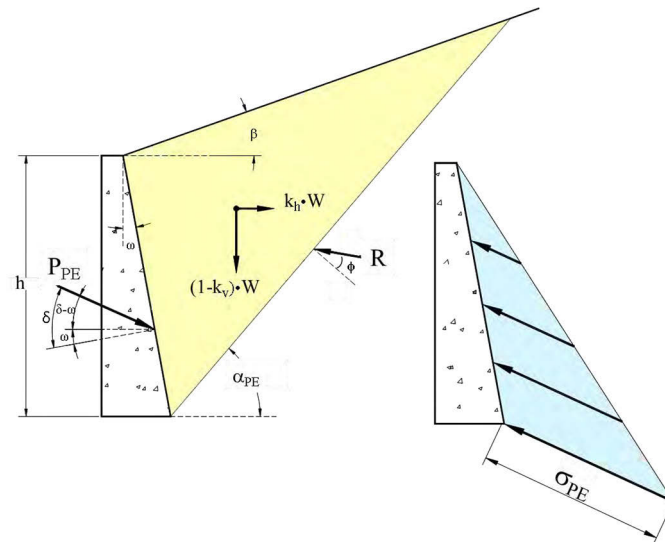


Figure 5. Mononobe-Okabe passive pressure (reproduced from [Shamsabadi et al., 2013])

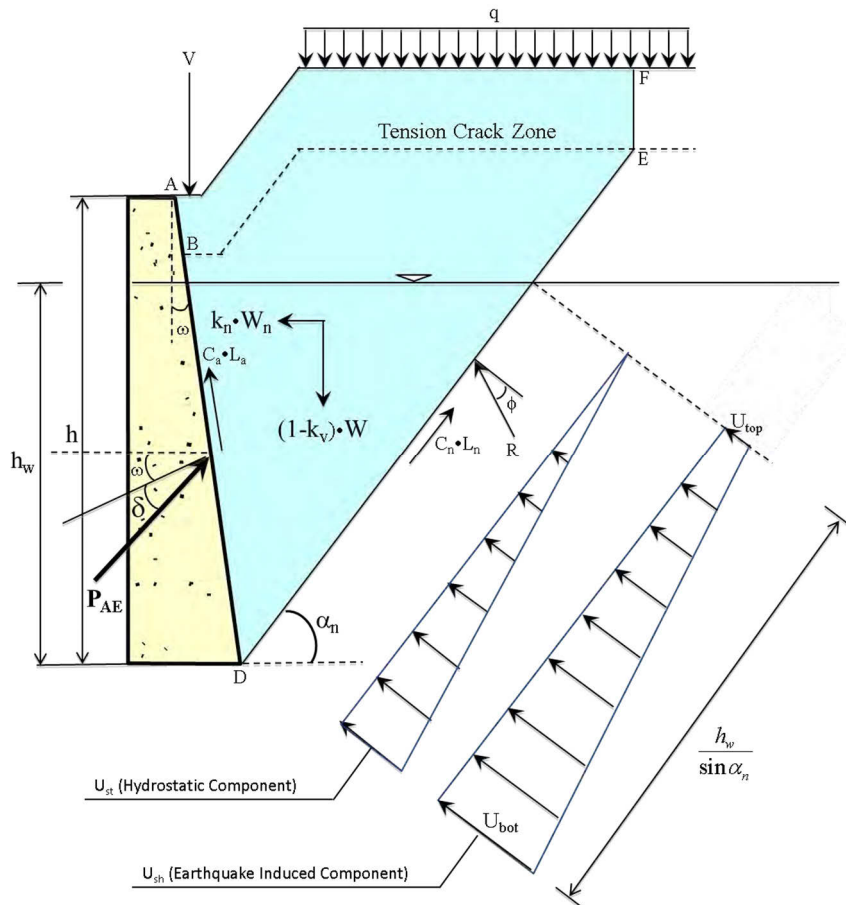


Figure 6. Trial wedge active pressure (reproduced from [Shamsabadi et al., 2013])

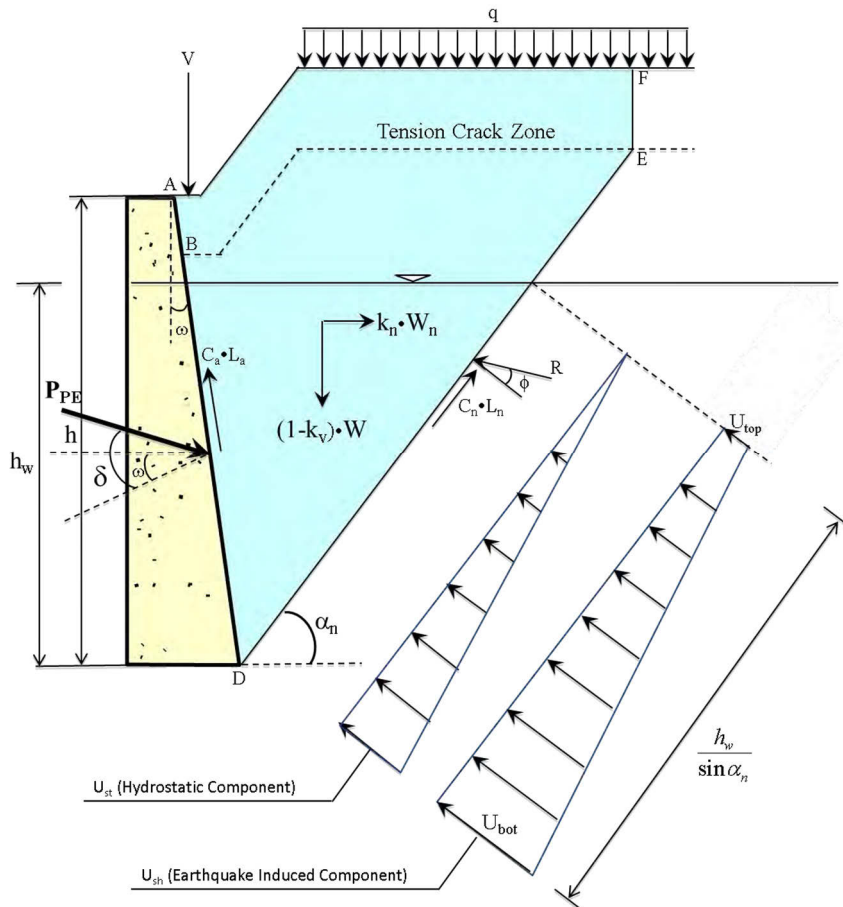


Figure 7. Trial wedge passive pressure (reproduced from [Shamsabadi et al., 2013])

There are a number of research studies on the shortcomings of force-based methods and advantages of displacement-based methods. Some findings from these research studies are summarized in the following:

### 2.1. National Guidance

**National Cooperative Highway Research Program. Report 611: Seismic analysis and design of retaining walls, buried structures, slopes, and embankments (2008)**

This report [Anderson et al., 2008] develops LRFD methods and specifications for the seismic analysis and design of retaining walls. It addresses the limitations of the Mononobe-Okabe and the trial wedge methods which Caltrans currently uses. It implies the need to better soil models which account for soil cohesion and assume a soil logarithmic-spiral failure surface. It briefly explains the potentials of using displacement-based methods and lowering seismic design coefficients.

**Federal Highway Administration.** *Publication FHWA-NHI-11-032: LRFD seismic analysis and design of transportation geotechnical features and structural foundations (2011)*

This publication [Kavazanjian et al., 2011] recognizes that a force-based method designs a structure to withstand peak earthquake loads. Such criterion, except for highly brittle structures, is overly conservative since it does not consider the transient nature of earthquake loads and that the duration of peak earthquake loads is short in comparison with permanent gravity loads. In reality, it is allowable to have substantial yielding in a ductile structure under extreme loads. Yielding will modify the dynamic behavior of the structure in a way that a reduction in the force demand from the assumed elastic behavior will be acceptable. Another consequence of yielding will be an increase in the fundamental period of the structure. As the fundamental period of the structure elongates, forces will usually decrease while displacements will usually increase. This phenomenon is illustrated in Figure 8.

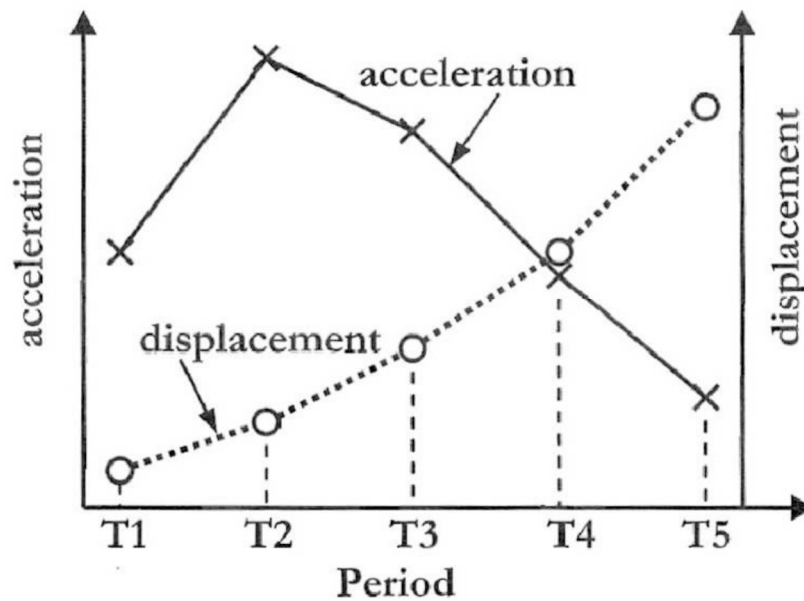


Figure 8. Acceleration and displacement design spectra (reproduced from [Kavazanjian et al., 2011])

This publication also recognizes that the trend is towards the use of displacement-based methods, but force-based methods will be needed where capacity protection and higher performance goals are necessary.

## 2.2. State Guidance

**California Department of Transportation.** *Final Report CA10-2039: Full-scale shake table test of retaining walls with and without sound wall (2011)*

This report [Mock & Cheng, 2011] is an experimental investigation of the seismic behavior of two retaining wall specimens by a full-scale shake table. The first specimen is a 6 ft tall semi-

gravity cantilever wall. The second specimen is identical to the first, but has an additional 6 ft tall sound wall on its top. The first specimen showed similar behavior to what had been simulated by the Mononobe-Okabe method. The second specimen, however, showed a non-linear pressure distribution along the height of the retaining wall. As a result, the Mononobe-Okabe method is not always appropriate to simulate the seismic behavior of retaining walls.

**California Department of Transportation. *Final Report CA13-2270: Development of improved guidelines for seismic analysis and design of earth retaining structures (2013)***

This report [Shamsabadi et al., 2013] presents Caltrans' current approach to the seismic analysis and design of earth retaining structures. It briefly explains a better soil model, i.e. the log-spiral-Rankine model [Shamsabadi et al., 2013b], which is especially preferable in passive pressure calculations. It also addresses the limitations of classical limit equilibrium methods for the performance-based design of retaining walls. An alternative approach to classical limit equilibrium methods is to use a beam-column-spring model. This model, which is illustrated in Figure 9, is also known as the "p-y" method. Using the continuum finite-element method is of course another alternative approach to classical limit equilibrium methods.

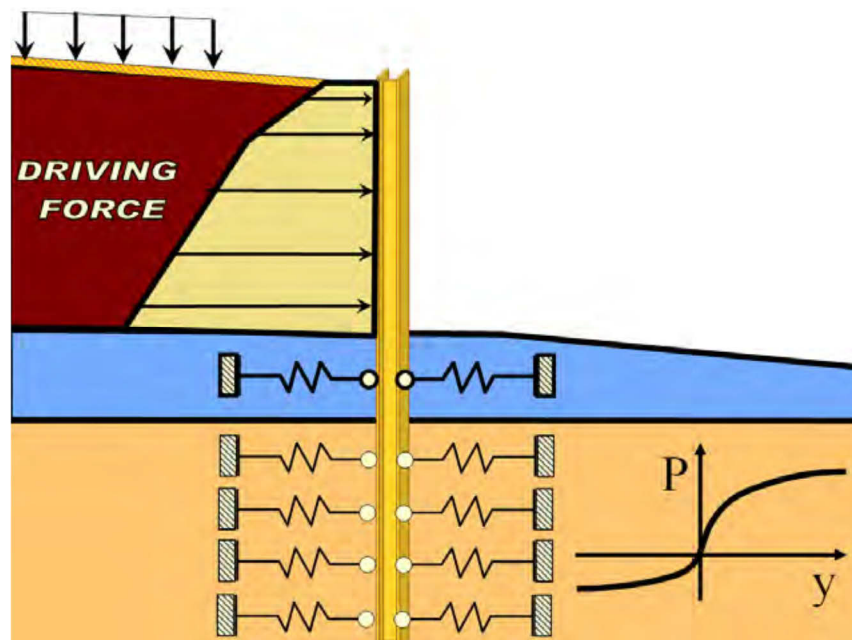


Figure 9. Conceptual "p-y" method for a cantilever retaining wall (reproduced from [Shamsabadi et al., 2013])

**California Department of Transportation. *Final Report CA13-2170: Seismic earth pressures on retaining structures in cohesive soils (2013)***

This report [Agusti & Sitar, 2013] includes experimental and numerical investigations of the seismic behavior of two centrifuge models. The first model consisted of a 6 m tall cantilever and a 6 m tall basement wall. The backfill in the first model was a horizontal silty clay soil. The

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second model consisted of a 6 m tall cantilever wall whose backfill was a sloped silty clay soil. Both models were also simulated by FLAC<sup>2-D</sup> with non-linear constitutive equations for soil and interface elements. The observations from the centrifuge experiments and the numerical simulations showed that both static and seismic soil pressures vary linearly with the height of the retaining wall. This report contains other recommendations for the seismic analysis and design of retaining walls, but also recognizes that the calculation of the seismic soil pressure remains to be a technical challenge and further research is needed.

### 2.3. Other Research

**Fragility curves for gravity-type quay walls based on effective stress analyses.** *Ichii K; 13th World Conference on Earthquake Engineering, Vancouver, British Columbia, Canada (2004)*

The definition of the performance-based design of retaining walls is still controversial. This paper is an example of studies where the permanent displacement of a retaining wall is defined to be the damage measure. It therefore implies the importance of displacement-based methods. The abstract of the paper is in the following:

*“Recent development of effective stress-based FEM analysis has enables seismic performance assessment of gravity-type quay walls for various geotechnical conditions. However, with these performance assessments using FEM, it is only possible to estimate the degree of deformation in a deterministic way, and another probabilistic procedure like the fragility curve approach is preferable in some case. This paper presents fragility-curves for gravity-type quay walls, which consider various design conditions including liquefaction resistance of foundations, based on results of FEM analyses.*

*A simple chart for seismic performance evaluation of gravity-type quay walls was proposed based on parametric study with an effective stress-based FEM. The chart can consider the effect of design seismic coefficient, liquefaction resistances of backfill and foundation soils, and depth of foundation layer. The applicability of the chart was verified with case histories. The results indicated that the chart could evaluate a wide range of displacement of quay walls, ranging from displacements in the order of one-tenth of meters to those one order higher, with an accuracy of twice or half order.*

*A damage level index based on the magnitude of seaward displacement for gravity-type quay wall was proposed based on restoration cost case histories. Considering the difference between the observed displacements in case histories and estimated displacements by the chart, a procedure to generate fragility curves for each damage level of gravity-type quay walls was proposed. And, fragility curves, which can consider the effect of design seismic coefficient, liquefaction resistances of backfill and foundation soils, and depth of foundation layer, were proposed as well.*

*The proposed fragility curves are quite useful for many situations, such as in the assessment of restoration cost after an earthquake, in the real-time damage level evaluation, and in the optimization of required seismic performance level based on cost-benefit analysis.”*



**A generalized log-spiral-Rankine limit equilibrium model for seismic earth pressure analysis.** Shamsabadi A, Xu SY, Taciroglu E; *Soil Dynamics and Earthquake Engineering*, 49: 197-209 (2013)

This paper offers an alternative to Caltrans' current approach (the Mononobe-Okabe and the trial wedge method) to the seismic analysis and design of earth retaining structures. The abstract of the paper is in the following:

*“A method of slices for estimating seismic earth pressures due to earthquake-induced pseudo-static body forces is presented herein. The method is based on a limit-equilibrium approach, and utilizes a composite logarithmic spiral failure surface along which the Mohr-Coulomb failure criterion is enforced. The model explicitly accounts for the magnitude of earthquake acceleration, the structure's height, the backfill soil properties (e.g., internal friction angle, and cohesion), and the mobilized interface friction angle between the backfill and the earth-retaining structure. Majority of the previous analytical (or semi-analytical) methods neglect the effects of soil's cohesion and/or use simple planar failure surfaces. Parametric studies conducted with the proposed method, as well as a number of prominent others indicate that the aforementioned simplifying assumptions often yield significantly different estimates of seismic earth pressures from the more general model proposed here, and that they may lead to sub-optimal or unsafe designs.”*

### **3. Gaps in Findings**

A brief synthesis of the existing knowledge on the seismic analysis and design of earth retaining structures was presented in Section 2. A number of gaps in the existing knowledge were also identified. A list of the identified gaps is as follows:

- Caltrans currently uses a force-based method for the seismic analysis and design of standard retaining walls. Studies [Ichii, 2004; Kavazanjian et al., 2011] show that this method is overly conservative.
- Caltrans does not currently have any guideline for the seismic analysis and design of pile-supported retaining walls.
- The current analysis and design of retaining walls in California use the Mononobe-Okabe and the trial wedge method. The soil failure in both methods is assumed to happen on a planar surface. Studies [Shamsabadi et al., 2013b] show that this soil model is simplistic especially in passive pressure calculations.
- The observations from the centrifuge experiments and the numerical simulations in [Agusti & Sitar, 2013] showed that both static and seismic soil pressures on a retaining wall vary linearly with its height. However, an experimental investigation of the seismic behavior of a retaining wall specimen by a full-scale shake table [Mock & Cheng, 2011] showed a non-linear pressure distribution along the height of the retaining wall. As a result, the calculation of the seismic soil pressure on retaining walls remains to be a technical challenge.
- Classical limit equilibrium methods have limitations for the performance-based design of retaining walls [Shamsabadi et al., 2013]. These methods assume that the retaining wall is

rigid, and do not properly model the interaction between the backfill and the retaining wall.

- In pile-supported retaining walls, the constituent interactions in the soil-pile-cap system have significant effects on the magnitude and the distribution of seismic soil pressures. As the retaining wall displaces in a seismic event, the constituent interactions, therefore the seismic soil pressure, will change. Force-based methods do not have the potential to capture these phenomena.

Research is needed to address these gaps, but the gaps are not limited to the above list. As a result of more research, more gaps may be identified and addressed.

#### **4. Next Steps**

Research is needed to address the gaps which were identified in Section 3, and to identify and address other gaps in the existing knowledge on the seismic analysis and design of earth retaining structures. A number of improvements were proposed in Section 2. A list of the proposed improvements is as follows:

- A new displacement-based method [Ichii, 2004; Kavazanjian et al., 2011] for the seismic analysis and design of standard and pile-supported retaining walls should be proposed. The new method should be readily applicable to Caltrans' practice. It should be also validated by existing experimental studies [Mock & Cheng, 2011; Agusti & Sitar, 2013] and verified against advanced numerical models [Agusti & Sitar, 2013].
- The new method should use an advanced soil model, e.g. the log-spiral-Rankine model [Shamsabadi et al., 2013b], which is especially preferable in passive pressure calculations. The soil model should be also validated by existing experimental studies [Agusti & Sitar, 2013].
- The new method should properly model the soil-wall interactions for all retaining walls and the soil-pile-cap interactions for pile-supported retaining walls. It should be also verified by advanced numerical methods, such as the "p-y" and the continuum finite-element method [Shamsabadi et al., 2013]. These advanced numerical methods should use pseudo-static as well as dynamic loadings.

The improvements are not limited to the above list. As a result of more research, more improvements may be proposed and implemented.

## 5. Contacts

The following people were consulted during the preparation of this report:

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## 6. References

Agusti GC, Sitar N (2013) Seismic earth pressures on retaining structures in cohesive soils. State of California Department of Transportation Final Report CA13-2170.

Anderson DG, Martin GR, Lam I, Wang JN (2008) Seismic analysis and design of retaining walls, buried structures, slopes, and embankments. National Cooperative Highway Research Program Report 611.

Ichii K (2004) Fragility curves for gravity-type quay walls based on effective stress analyses. 13th World Conference on Earthquake Engineering, Vancouver, British Columbia, Canada.

Kavazanjian E, Wang JN, Martin GR, Shamsabadi A, Lam I, Dickenson SE, Hung CJ (2011) LRFD seismic analysis and design of transportation geotechnical features and structural foundations. Federal Highway Administration Publication FHWA-NHI-11-032.

Mock E, Cheng LD (2011) Full-scale shake table test of retaining walls with and without sound wall. State of California Department of Transportation Final Report CA10-2039.

Shamsabadi A, Xu SY, Taciroglu E (2013) Development of improved guidelines for seismic analysis and design of earth retaining structures. State of California Department of Transportation Final Report CA13-2270.

Shamsabadi A, Xu SY, Taciroglu E (2013b) A generalized log-spiral-Rankine limit equilibrium model for seismic earth pressure analysis. *Soil Dynamics and Earthquake Engineering*, 49: 197-209.

State of California Department of Transportation (2014) Design criteria of standard earth retaining systems. State of California Department of Transportation Memo to Designers 5-5.

## **Appendix A**

State of California Department of Transportation Memo to Designers 5-5

Design criteria of standard earth retaining systems

# Appendix A

State of California  
DEPARTMENT OF TRANSPORTATION

Business, Transportation and Housing Agency

## Memorandum

*Serious drought.  
Help Save Water!*

To: MICHAEL KEEVER  
ROBERT STOTT  
PHILIP STOLARSKI  
SHIRA RAJENDRA  
DOLORES VALLS

Date: April 9, 2014

From: BARTON NEWTON  
Deputy Division Chief  
Structure Policy and Innovation  
Division of Engineering Services



Subject: **NEW MEMO TO DESIGNERS 5-5 “DESIGN CRITERIA OF STANDARD EARTH RETAINING SYSTEMS”**

This new *Memo to Designers 5-5* (MTD 5-5) “Design Criteria of Standard Earth Retaining Systems” documents material parameters and assumptions made in the development of the standard earth retaining systems (ERS) found in the 2010 *Standard Plans*, 2010 Revised Standard Plans and the most recent Bridge Design Detail Sheets (XS). To comply with the FHWA mandate for designing ERS using load and resistance factor design (LRFD) methodology by October 2010, all of the standard ERS were designed to the *AASHTO LRFD Bridge Design Specifications* (4<sup>th</sup> edition, 2007) and the corresponding California Amendments.

MTD 5-5 and these standards will remain in effect for use, after Caltrans adopts the *AASHTO LRFD Bridge Design Specifications, 2012 (6<sup>th</sup> edition) with CA Amendments (AASHTO-CA BDS-6)* and the 2015 (Caltrans) *Standard Plans and Standard Specifications*. As time and resources permit, updates may be done for *AASHTO-CA BDS-6*.

Users of these standards should be aware that projects often possess conditions that are in conflict with the design parameters and assumptions employed in the standard ERS. Special design should be carried out under these circumstances.

Any inquiry regarding and interpretation of MTD 5-5 should be addressed to Kathryn Griswell, the chair of the Earth Retaining Systems Committee, at 916-227-7330.

Cc: Tim Craggs, Chief, Division of Design  
Ray Zhang, Chief, Division of Local Assistance  
Susan Hida, Chief, Office of State Bridge Engineer Support  
Kathryn Griswell, Technical Specialist, State Bridge Engineer Support  
Gary Wang, Technical Specialist, State Bridge Engineer Support

*“Provide a safe, sustainable, integrated and efficient transportation system  
to enhance California’s economy and livability.”*



## 5-5 DESIGN CRITERIA OF STANDARD EARTH RETAINING SYSTEMS

### Introduction

With the implementation of AASHTO Load and Resistance Factor Design (LRFD) Bridge Design Specifications (AASHTO Design Specifications) a new set of Earth Retaining Systems (ERS) have been produced and published as Standard Plans or Revised Standard Plans. Similarly, a new set of Bridge Standard Details (XS sheets) related to ERS have been produced and added to the working set of Bridge Standard Details. This memo summarizes the design criteria and assumptions used to produce the new plans. This memo is not intended to include every aspect of design in the AASHTO Design Specifications, nor is this memo intended as a substitute for the AASHTO Design Specifications.

The design parameters for design of these ERS are based on the AASHTO Design Specifications, 4<sup>th</sup> edition, 2007, and the 2010 California Amendments (California Amendments).

ERS that appear as 2010 Standard Plans or Revised Standard Plans are:

- Retaining Walls – Type 1, 1A, 5 and 6
- Crib Walls – made of reinforced concrete or steel

ERS that appear as Bridge Standard Details are

- Retaining Walls – Type 7
- Modified Retaining Walls supporting sound walls, Type 1SW series and Type 5SW series and Type 7SW series
- Mechanically Stabilized Embankment (MSE)

### Design Parameters and Assumptions

#### a) Material Properties

The soil parameters and material properties assumed for design purposes are consistent with the 2010 Standard Specifications and Standard Special Provisions. Accordingly, these values are the default values utilized in the design of the Standard Plans and the Bridge Standard Details. Project specific parameters must be used when materials available for use on that project result in greater force effects on ERS, and the standard designs should be re-evaluated for the project in such cases.



### *Soil Backfill Parameters*

- Unit Weight of Soil,  $\gamma_s = 120$  pcf
- Soil Cohesion,  $c = 0$
- Internal friction angle,  $\phi = 34^\circ$  for the backfill and foundation soil of all ERS except MSE
- Internal friction angle,  $\phi = 34^\circ$  for the reinforced soil of MSE
- Internal friction angle,  $\phi = 30^\circ$  for the retained soil (behind the reinforced soil) and foundation soil (below the reinforced soil) of MSE

### *Material Properties of Reinforced Concrete Elements*

- Compressive Strength of Concrete at 28 days,  $f'_c = 3.6$  ksi (4.0 ksi for MSE panels)
- Reinforced Concrete Unit Weight,  $\gamma_c = 150$  pcf
- Minimum Yield Strength of Reinforcing Steel,  $f_y = 60$  ksi

### b) Drainage and Compaction

Sufficient and appropriate drainage details are assumed to be provided in the reinforced soil and the retained soil. Hence no water pressure is considered in the design. Also, no compaction loads are considered in the design, since the construction methods allowed in the Standard Specifications prevent inducing any additional stress in the structures.

## Standard Design Considerations

### a) Limit States and Load Combinations

Service Limit State I, Strength Limit State I and Extreme Event Limit State I (earthquake) shown in Table 3.4.1-1 of the California Amendments were considered for design of all standard ERS retaining backfill supporting highway traffic. Note that load combination Strength IV in Table 3.4.1-1 is not applicable to ERS. The load combinations used were,

#### *Service Limit State I*

$$1.0DC+1.0EV+1.0EH +1.0LS$$





*Strength Limit State I*

$$1.25DC + 1.35EV + 1.5EH + 1.75LS \quad \text{for Ia (bearing, structure capacity)}$$

$$0.90DC + 1.00EV + 1.5EH + 1.75LS \quad \text{for Ib (sliding, bearing, structure capacity)}$$

*Extreme Event Limit State I*

$$1.0DC + 1.0EV + 1.0EH + 1.0EQE + 1.0EQD \quad \text{for all ERS except crib walls}$$

$$1.0DC + 1.0EV + 1.0EH + 1.0EQE \quad \text{for crib walls}$$

(For Extreme Event Limit State I, live load surcharge is not considered)

where:

*DC* = the self weight of structural components

*EV* = the self weight of the soil above the heel of a footing in a semi-gravity retaining wall or of the reinforced soil in a MSE

*EH* = static soil lateral load

*LS* = live load surcharge

*EQE* = dynamic soil lateral load

*EQD* = the inertia from *EV* and *DC*. Numerically, *EQD* is equal to the horizontal seismic coefficient,  $k_h$ , times *EV* plus  $k_h$  times *DC* except for the case of the crib walls, where *EQD* equals  $k_h$  times *EV*

More information about Extreme Event Limit State I can be found in section d) Seismic Design.

At the Service Limit State, the ERS is evaluated for eccentricity, and structural service performance, such as member deformation (e.g. the stem deflection on a Type 1 wall), cracking, temperature, and shrinkage requirements (in the case of the standard ERS built with reinforced concrete). At the Strength Limit States, the ERS is evaluated so that sliding limits and structural strength are not exceeded. At Extreme Event Limit State I, the ERS is evaluated so that eccentricity, sliding limits, and structural strength are not exceeded. The bearing stresses of each ERS are provided for project specific use of all standard ERS designs. Similarly, overall stability and settlement must be considered for project specific use of these designs. Table 1 summarizes design considerations for all standard ERS.



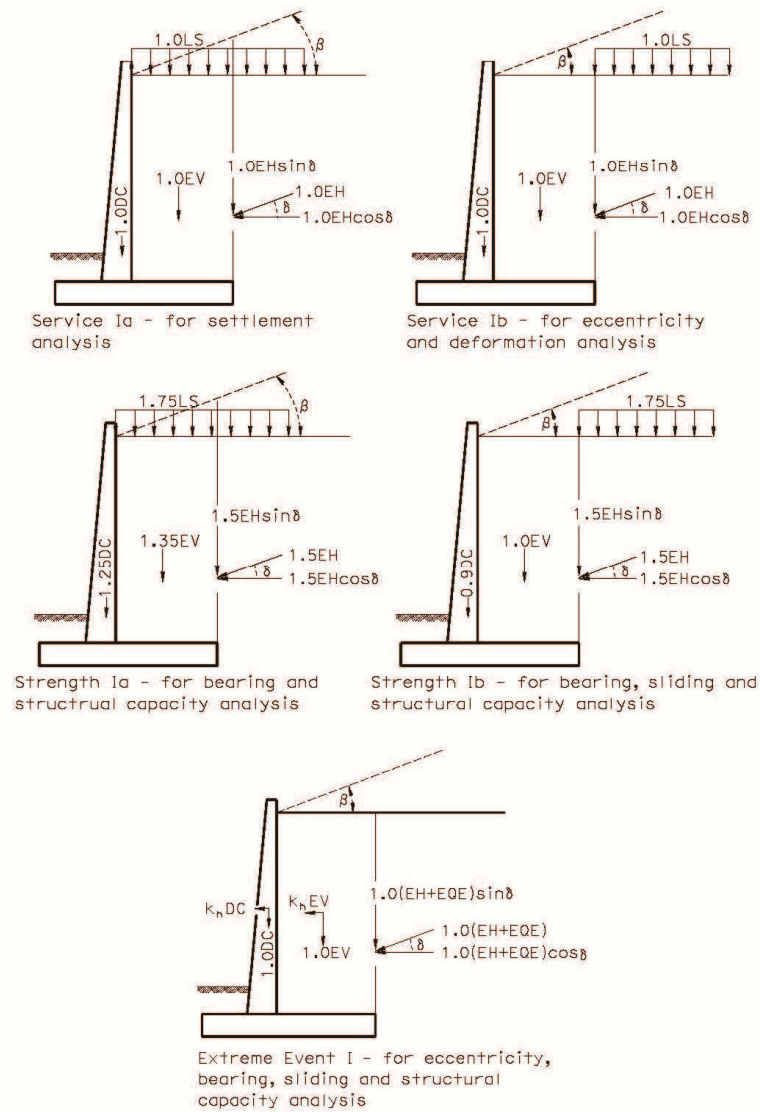
**Table 1 Analysis for ERS Design**

Limit State	Service I	Strength Ia	Strength Ib	Extreme Event I (Seismic)
Bearing Stresses*	X	X	X	X
Eccentricity	X			X
Sliding			X	X
Structural Service Performance	X			
Structural Capacity		X	X	X

\* To be checked against actual project conditions before use of the Standard

Load combinations for concrete retaining walls supporting sound walls or containing ground anchors have slightly different load combinations than other standard ERS. The load combinations for those ERS include force effects of the wind load on the sound wall, the inertial force of the sound wall for seismic events, and the prestress force from the vertical ground anchors. These walls form part of the Bridge Standard Details (XS sheets), and their respective loading can be found on those sheets.

Load factors are chosen to create maximum force effect for a given load combination. Strength Limit State I is separated into Strength Ia and Strength Ib using load factor values as shown in Figure 1. These load combinations are also illustrated in Section C11.5.5 of the AASHTO Design Specifications. The loads depicted in Figure 1 are shown applied to a semi-gravity wall, but are applied to all standard ERS.



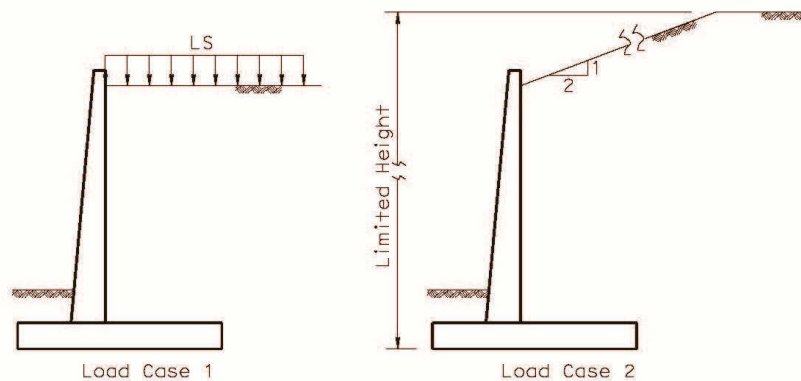
**Figure 1 Limit States and Load Combinations**



### b) Standard Loading Cases

The loading case numbers (i.e. Case 1, Case 2, and Case 3) assumed in the standard designs should not be confused with the limit state load combination numbers in the LRFD methodology previously discussed. The standard loading cases depict the backfill and live load surcharge configurations used in the design. There are two standard loading cases, Load Case 1 and Load Case 2. Load Case 1 has a traffic live load on a horizontal backfill, and Load Case 2 has a backfill slope of two horizontal to one vertical (2:1) for a specified distance and then turns level afterwards.

Minor variations in loading cases occur according to ERS types. Some standard ERS have additional loading cases that are considered and are shown on the respective standards. When additional project specific loading is required on the ERS, the standard designs can no longer apply to the project without special design. The standard loading cases are shown in Figure 2.



**Figure 2 Standard Loading Cases**

### c) Live Load Surcharge

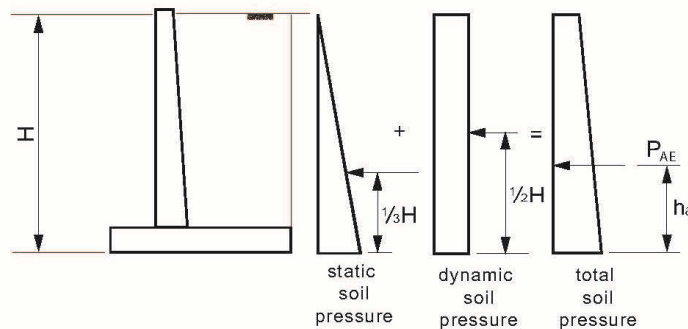
The Live Load Surcharge is positioned to produce the maximum design load. In Figure 1, where a semi-gravity wall is shown, the Live Load Surcharge is placed over any element of the ERS for settlement and bearing analysis, while the Live Load Surcharge is placed behind all the elements of the ERS for sliding, and eccentricity analysis. Note that the Live Load Surcharge is not applied to the sloped portion of the backfill depicted by the dashed lines in Figure 1, or anywhere on the backfill for Extreme Event Limit State I.



### d) Seismic Design

The seismic design of the standard ERS is performed using either Mononobe-Okabe (MO) Method for Loading Case 1 (a backfill with a planar surface and no live load surcharge), or the trial wedge method for Loading Case 2. The Trial Wedge Method is similar to the MO Method and is used for the other Loading Cases where the backfill surface is not planar.

As a result of analysis using the MO Method, the resultant of seismic soil pressure,  $P_{AE}$  is obtained. All standard ERS are designed using the criteria in the 2010 California Amendments for seismic load. The 2010 California Amendments assumes that the total soil thrust,  $P_{AE}$  is separated into two components, the static active soil pressure in a triangular shape and the dynamic soil pressure in a rectangular shape, as shown in Figure 3.



**Figure 3 Seismic Loading**  
(Reference: 2010 California Amendments)

Therefore, the total soil lateral load estimated using the MO method or a similar trial wedge method was a function of the horizontal seismic coefficient,  $k_h$ , the vertical seismic coefficient,  $k_v$ , and the soil internal friction angle,  $\phi$ . However,  $k_v$  was assumed to be zero for most cases because horizontal and vertical accelerations are assumed not to occur simultaneously. For a large  $k_h$  or for an infinitely long and steep backfill slope, numerical difficulty occurs and both the MO method and the trial wedge methods yield no solution. In reality a slope is seldom infinitely long. The numerical difficulty can then be circumvented by assuming the backfill surface levels off after rising to a specified height above the ERS so the trial wedge method can be employed.

Most standard ERS are designed assuming a  $k_h$  equal to 0.2, except for concrete retaining walls supporting sound walls where a  $k_h$  of 0.3 is assumed in the design. A  $k_h$  of 0.2 is usually adequate for ERS built in most parts of California where no additional surcharges are present or structure movements are not restricted. When the inertia of the structural member and the



affected soil is included in the seismic design, the inertial force is assumed to act at their respective center of gravity.

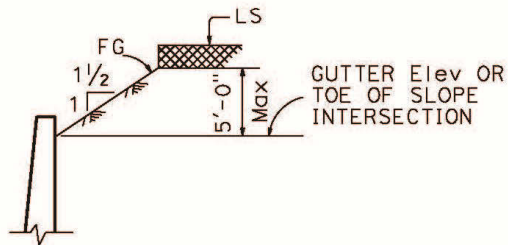
## ERS Type-Specific Design Considerations

The following describes design assumptions specific to various ERS types.

### a) Semi-Gravity Retaining Walls

#### *Additional Loading Case*

In the case of semi-gravity concrete retaining walls such as Standard Plan Type 1, there is an additional loading case considered. Along with Load Case 1 - Horizontal Backfill, and Load Case 2 - Sloped Backfill of 2 horizontal to 1 vertical and limited to a vertical height of 40 feet for the slope, there is also a Load Case 3 with a broken sloped backfill up to 5 feet, as shown in Figure 4.



**Figure 4 Loading Case 3 for Type 1 and Type 5 Retaining Walls**

#### *Live Load Surcharge*

The effect of the design truck and design lane on soil acting on the ERS for Load Case 1 has been considered by applying an equivalent uniform soil layer on top of the retained soil, and has been defined as Live Load Surcharge (*LS*). The depth of such a layer depends on the distance from the edge of the traffic to a vertical line where the soil pressure is evaluated and on the height of the ERS. Table 3.11.6.4-2 in the AASHTO LRFD Design Specifications (2007) lists equivalent soil heights for vehicular loading on ERS.



### *Sliding Resistance*

For semi-gravity walls sliding resistance is provided by passive resistance on the footing and shear key, as well as the friction between the footing and the foundation soil. When calculating the passive resistance, the passive force provided by the soil over the top of the footing is ignored because the material in this region is often disturbed and hence the passive force of this region is not reliable. However, the contribution of the weight of this portion of the soil is considered in calculating the passive resistance of the soil in front of the footing and the shear key. Figure 5 shows how the passive resistance is calculated. The arrows in the pressure diagram in front of the footing and the shear key denote the passive pressure contributing to the passive resistance. (For other types of ERS the passive resistance is ignored and only the friction at the bottom of the wall is considered in resisting sliding.)

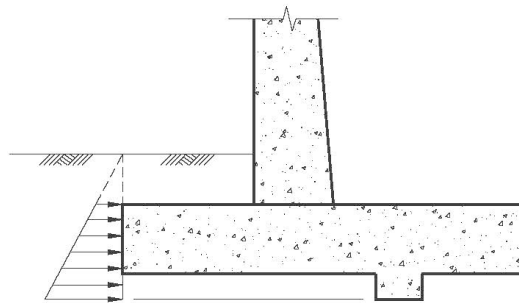


Figure 5 Passive Resistance on Footing and Shear Key

In the past, friction resistance at the bottom of a semi-gravity wall was provided by two separate parts, all being a function of the magnitude of the normal pressure on the bottom of the footing. The first part was based on the friction from the toe to the left edge of the shear key. A coefficient of friction equal to the tangent of the soil friction angle was used when calculating this part of the friction resistance. The second part was based on the friction for the remainder of the footing width, using a coefficient of friction equal to the tangent of two-thirds the soil friction angle. The first part was assumed to be based on soil-on-soil friction, while the second part was based on soil-on-footing friction. The bottom of the footing, however, is rough, unlike other parts of the wall such as the stem with smooth surfaces. Hence the reduced friction coefficient of the second part is not warranted. The friction coefficient for the 2010 semi-gravity walls is assumed to be the same along the entire width of the footing and is not reduced.



### *Extreme Event Limit State II*

In the case of semi-gravity concrete walls with level backfill on which highway traffic is present, solid traffic barriers (e.g. type 736, 742, etc.) may be integrally mounted on top of the stem. The vehicular collision force on the barrier must be considered in the design of the walls. This load combination falls in the category of extreme event limit state II, hence the load factor is 1.0. Live load surcharge is not considered in this load combination. The load combination involving vehicular collision in standard plan wall design is,

$$1.0EH+1.0DC+1.0EV+1.0CT$$

where:

$CT$  = the vehicular collision load of 54 kips corresponding to a Test Level 4 load

At Extreme Event Limit State II, the ERS is evaluated so that bearing capacity, sliding requirements, and structural strength are not exceeded.

The collision force ( $CT$ ) is assumed to be distributed over a length of 10 feet at top of the stem for a solid barrier and is assumed to spread downward to the top of the footing at a 45 degree angle. The spread limits thus constitute the contributory length of the wall resisting the collision force. Figure 6 illustrates how the collision force is distributed down the wall stem. The shaded area illustrates the effective region resisting the collision force. In Figure 6,  $F_c$  is the lateral design collision load and is 54 kips corresponding to Test Level 4 (TL4).  $\theta_c$  is the angle of the collision load spread down the wall which is assumed to be 45 degrees and  $L_c$  is the length over which the collision load is spread at the top of the stem and is assumed to be 10 feet. When calculating the moment of the stem, the moment arm is measured from 32 inches above the toe of the barrier to the point on the stem where the moment is evaluated.



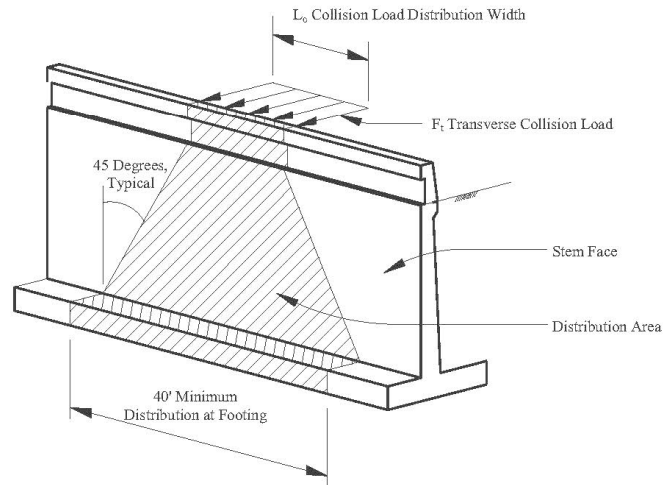
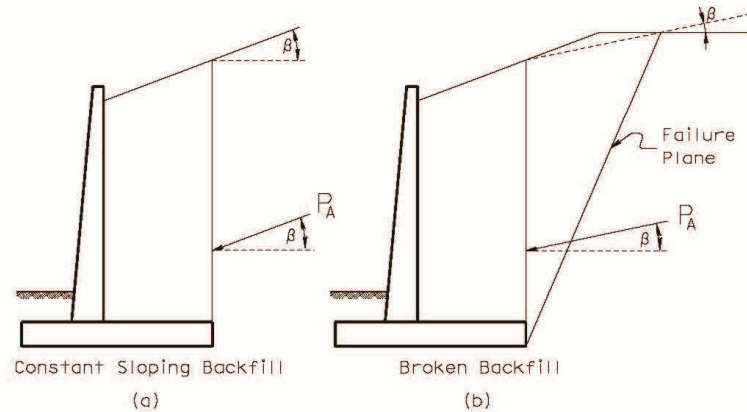


Figure 6 Collision Force Distributions

### Orientation of $P_A$ and $P_{AE}$

When analyzing for external stability, the soil pressure on a semi-gravity retaining wall is usually evaluated at a vertical plane that passes through the back of the heel. This vertical plane is shown as a solid line in Figure 7(a) and (b). Figure 7(a) shows a sloped backfill surface, and  $\beta$  is the slope of the surface from horizontal. Figure 7(b) shows a broken back backfill, and  $\beta$  is assumed to be equal to the angle, from horizontal, of a fictitious slope formed by a line connecting the point where the vertical plane passing through the heel and the backfill surface intersect, and the point where the failure plane in the backfill and the backfill surface intersect. The failure plane is determined by the trial wedge method. The direction of  $P_A$  or  $P_{AE}$  is assumed to be equal to  $\beta$  for all limit state analyses as shown in Figure 7. In Figure 7 only  $P_A$  is shown, the direction of  $P_{AE}$  is similar.



**Figure 7** Direction of  $P_A$  or  $P_{AE}$  for Semi-Gravity Walls

### *Temperature and Shrinkage Reinforcement*

The amount of the temperature and shrinkage reinforcement in the footing along the length of the wall is equally distributed at the top and the bottom surfaces of the footing. The stem is divided into several zones according to the stem thickness. Two thirds of this reinforcement is placed at the front face of the stem that is exposed to the elements and the remaining on the backfill side. Layout of the reinforcement is consistent with the long time practice for this type of the retaining walls developed by the Caltrans, and with the provisions in ACI 318-08.

### b) Concrete Crib and Steel Bin Walls

Concrete crib and steel bin walls are old technology, therefore, only the basic AASHTO design provisions are provided for these designs. Consequently, the modified silo theory was utilized for the design of both the steel bin and the concrete open crib and closed crib walls. Standard timber walls were discontinued due to durability, redundancy, and fire resistance concerns.

In silo theory a portion of the weight of the backfill “soil plug” in the center of the bin or crib loads the walls through frictional contact with the rough and irregular surface of the walls composing the bin or crib. The rest of the “soil plug” rests on the foundation soil through the open bottom. These combine to create a highly irregular contact pressure diagram. A generalized uniform pressure is reported for practical application.

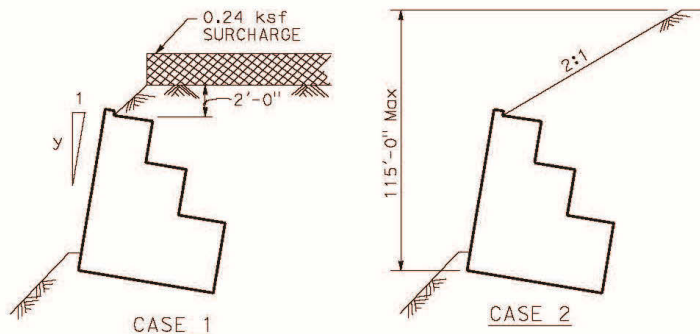


Designing the base of the walls of the bin or crib is difficult as the mathematical analyses often indicates that failure will occur but is not seen in practice when constructed on yielding foundation soils. Therefore, the design assumes the foundation soil must give sufficiently to allow the corner base plate or bottom most crib member to slightly punch into the foundation soil enough to transfer the loading back to the “soil plug” and avoid deformation failure. This design cannot be used directly on solid rock, nor a concrete slab, without a special soil layer designed as its foundation.

Drainage must be provided in these designs especially when the facing closure member is selected for use. The special backfill gradation in the construction specifications typically provides for sufficient drainage in open cribs and bins from within the structure. The materials behind and underneath must still be adequately drained for the unsaturated conditions assumed during design. Care must be taken when selecting a different backfill for inside these systems so that both the weight and the drainage requirements are maintained.

No collision loading on traffic barriers or rail is included in these designs. The Load Case 1 condition is modified to provide sufficient soil separation from the traffic to the top members of the bin or crib. Additionally, one of the benefits of these designs is the ability to deform in service. All design details are modeled as pinned to maintain this deformation ability. Support of any rigid loading physically attached to these structures was not considered in design and doing so would constitute a special design. Historically this type of loading has not been allowed.

In the case of the Concrete Crib Walls and the Steel Bin Walls, Load Case 1 includes a slight variation of the backfill to provide two feet clearance above the structural members for Metal Beam Guardrail or Concrete Barrier installation, as shown in Case 1 of Figure 8. In addition, the back slope of Load Case 2 is limited to only 115 feet above the base, as shown on the right side of Figure 8.

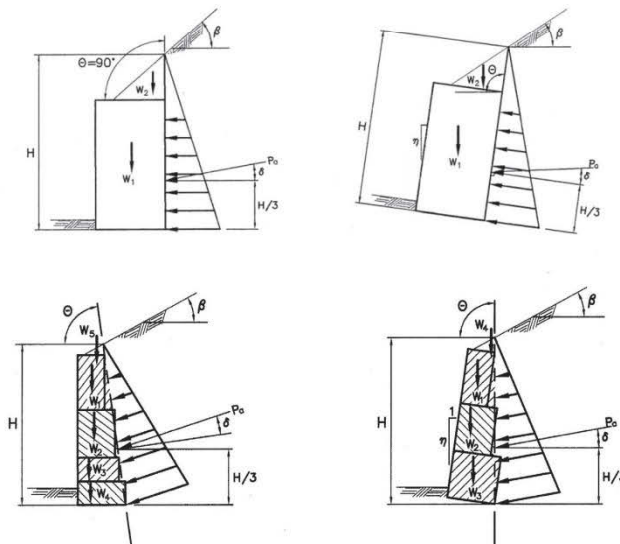


**Figure 8 Variations in Loading Cases for Crib and Bin Walls  
(Reference: Standard Plan C7C)**



### Orientation of $P_A$ and $P_{AE}$

In the case of single cell crib and bin walls, the plane where the soil lateral pressure is applied is the backside of the cell. The  $\delta$  for  $P_A$  and  $P_{AE}$  is taken as 0.5 of the soil friction angle,  $\phi$ . In the case of multiple cell crib walls, the plane of soil lateral pressure application is a plane connecting the top back corner of the topmost cell and the bottom back corner of the bottom cell, as shown in Figure 9. The  $\delta$  for  $P_A$  and  $P_{AE}$  is taken as 0.75 of  $\phi$ .



**Figure 9 Single and Multiple Cell Crib and Bin Walls  
(Reference: AASHTO 2007)**

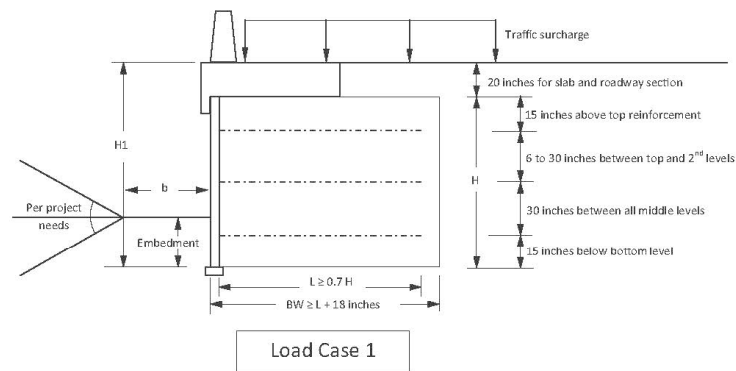
### c) Mechanically Stabilized Embankment (MSE)

In the case of MSE, the Coherent Gravity Method (CGM) is utilized for internal design with metallic soil reinforcement. All the resistance factors for the tensile resistance of the soil reinforcement and connections are amended. Refer to Table 11.5.6-1 and Section 11.5.7 in the California Amendment for the resistance factor values.

The design life of the MSE soil reinforcement is increased to 75 years.



For Load Case 1, the standard MSE design height is increased by 1'-8", measured from the top of the top panels to the roadway surface, in order to accommodate the traffic barrier attached to a concrete slab floating above the MSE. The concrete barrier slab design used is shown on XS12-090. The increase over prior practice will also reduce the potential conflict between the roadbed base layers and the reinforcement by providing typically 35 inches of cover over the topmost layer of soil reinforcement, as shown in Figure 10. This change increases the overburden pressure used in the design of the MSE in addition to the live load surcharge. For Load Case 2 the simple coping remains the same as in prior practice, no additional height was utilized.



**Figure 10 Additional Overburden Height for Roadbed and Barrier Slab  
(Reference BDA 3-8)**

The base width (*BW*) in Figure 10 is no longer synonymous with the length of the soil reinforcement. The design assumes the *BW* will be used to set the MSE on site and move utilities, sign foundations and so forth as needed. The *BW* includes the facing thickness, the reinforcement length, and at least 1 foot of the reinforced backfill behind the end of the steel reinforcement which separates the reinforcement from the retained backfill that might be chemically aggressive to the steel. *BW* in Figure 10 assumes a panel thickness of 6 inches.

Passive pressure is ignored at the front base of the MSE during all stability analyses, since erosion and various maintenance activities can remove the fill during the MSE's service life. A minimum embedment is still required to reduce the potential of undermining at the toe during the MSE's service life.

No vehicular collision loading is applied to the MSE. The barrier slab system is placed on top in the Load Case 1 condition. Under collision forces, the dynamic analysis of the barrier



slab shows that the vehicle briefly lost contact with the slab during collision when it was redirected back onto the roadway. This temporarily lifts the slab slightly from the backfill soil and negates friction force transfer into the MSE. Additionally, the notch used to recess the top panels into the slab in the previous design has been removed from the bottom of the slab to disengage the load transfer to the back of the facing panels. If the slab is to be buried and rotation off the soil is prevented, the MSE will need to be specially designed to include the collision load.

The 2010 Standard Specifications for construction of MSE allow for finer soils with slightly more aggressive corrosion behavior than the AASHTO construction specifications during design. Thus the MSE design continues to apply the corrosion loss equations that correspond to these more aggressive backfill soils (California Amendments 11.10.6.4.2a). It is anticipated that the backfill soil specifications will be revisited after the corrosion study into the actual lifetime corrosion of metallic MSE reinforcement in California is complete.

Bridge Design Aids 3-8 contains information about standard MSE using 5ft by 5ft concrete panels and steel soil reinforcement. The MSE design details, design considerations, inspection wire locations and internal drainage requirements and design check lists can also be found in BDA 3-8.



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